Fractions, Decimals and Percentages (H)

## Intervention Booklet

Name:

Class:

## Useful websites:

www.mathswatchvle.com
(Video explanations and questions)
Username: STH...@twgash
Password: stmaths
www.methodmaths.com
(Past papers online that get instantly marked)
Centre ID: wga
Username: firstname
Password: lastname
www.hegartymaths.com
(Online tutorials and quizzes)
Login: first name and last name are case sensitive
www.bbc.co.uk/schools/gcsebitesize/maths

## Percentages of Amounts, Increasing and Decreasing

## Things to remember:

- "Per cent" means "out of 100 ".
- Increase means the value will go up, decrease means the value will go down.


## Questions:

1. David is going to buy a cooker.

The cooker has a price of $£ 320$
David pays a deposit of $15 \%$ of the price of the cooker.
How much money does David pay as a deposit?
£ $\qquad$
(Total for Question is 2 marks)
2. Work out $65 \%$ of 300
(Total for question = 2 marks)
*3. Barak is going to buy 550 nails from one of these companies.

| Nail Company |
| :---: |
| 50 nails |
| $£ 4.15$ plus VAT at $20 \%$ |
|  |

## Hammer Company

25 nails
£2.95

Special offer
Buy 100 get 25 free

He wants to buy the nails at the cheaper cost.
Where should he buy the nails, from the Nail Company or the Hammer Company?
4. Greg sells car insurance and home insurance.

The table shows the cost of these insurances.

| Insurance | car insurance | home insurance |
| :--- | :--- | :--- |
| Cost | $£ 200$ | $£ 350$ |

Each month Greg earns
$£ 530$ basic pay
$5 \%$ of the cost of all the car insurance he sells
and $10 \%$ of the cost of all the home insurance he sells
In May Greg sold
6 car insurances
and 4 home insurances
Work out the total amount of money Greg earned in May.
5. Mr Watkins needs to buy some oil for his central heating.

Mr Watkins can put up to 1500 litres of oil in his oil tank.
There are already 850 litres of oil in the tank.
Mr Watkins is going to fill the tank with oil.
The price of oil is 67.2 p per litre.
Mr Watkins gets $5 \%$ off the price of the oil.
How much does Mr Watkins pay for the oil he needs to buy?
*6. Jim's pay is $£ 180$ each week.
Jim asks his boss for an increase of $£ 20$ a week.
Jim's boss offers him a 10\% increase.
Is the offer from Jim's boss more than Jim asked for?
You must show your working.
(Total for Question is 3 marks)
*7. Gordon owns a shop.
Here are the prices of three items in Gordon's shop and in a Supermarket.

| Gordon's Shop |  |
| :--- | :--- |
|  |  |
| 400 g loaf of bread | $£ 1.22$ |
| 1 litre of milk | $£ 0.96$ |
| 40 tea bags | $£ 2.42$ |


| Supermarket |  |
| :--- | :--- |
|  |  |
| 400 g loaf of bread | $£ 1.15$ |
| 1 litre of milk | $£ 0.86$ |
| 40 tea bags | $£ 2.28$ |

Gordon reduces his prices by $5 \%$.
Will the total cost of these three items be cheaper in Gordon's shop than in the Supermarket?
8. Mr Brown and his 2 children are going to London by train.

An adult ticket costs $£ 24$
A child ticket costs $£ 12$
Mr Brown has a Family Railcard.

## Family Railcard gives

$\frac{1}{3}$ off adult tickets
$60 \%$ off child tickets

Work out the total cost of the tickets when Mr Brown uses his Family Railcard.
$£$.
(Total for Question is 4 marks)

## Percentages - compound interest

## Things to remember:

- New amount $=$ original amount x multiplier ${ }^{n}$


## Questions:

1. Henry invests $£ 4500$ at a compound interest rate of $5 \%$ per annum.

At the end of $n$ complete years the investment has grown to $£ 5469.78$.
Find the value of $n$.
2. Bill buys a new machine.

The value of the machine depreciates by $20 \%$ each year.
(a) Bill says 'after 5 years the machine will have no value'. Bill is wrong. Explain why.
$\qquad$
$\qquad$
$\qquad$
Bill wants to work out the value of the machine after 2 years.
(b) By what single decimal number should Bill multiply the value of the machine when new?
$\qquad$
3. Gwen bought a new car. Each year, the value of her car depreciated by $9 \%$.

Calculate the number of years after which the value of her car was $47 \%$ of its value when new.
4. The value of a car depreciates by $35 \%$ each year.

At the end of 2007 the value of the car was $£ 5460$ Work out the value of the car at the end of 2006
$\qquad$
5. Toby invested $£ 4500$ for 2 years in a savings account.

He was paid $4 \%$ per annum compound interest.
(a) How much did Toby have in his savings account after 2 years?
$£$
Jaspir invested $£ 2400$ for $n$ years in a savings account.
He was paid $7.5 \%$ per annum compound interest.
At the end of the $n$ years he had $£ 3445.51$ in the savings account.
(a) Work out the value of $n$.
6. Mario invests $£ 2000$ for 3 years at $5 \%$ per annum compound interest.

Calculate the value of the investment at the end of 3 years.
$£$
(Total 3 marks)
7. Toby invested $£ 4500$ for 2 years in a savings account.

He was paid $4 \%$ per annum compound interest.
How much did Toby have in his savings account after 2 years?
$£$

## Percentages - reverse

## Things to remember:

- Work out what the multiplier would have been;



## Questions:

1. Loft insulation reduces annual heating costs by $20 \%$.

After he insulated his loft, Curtley’s annual heating cost was $£ 520$.
Work out Curtley's annual heating cost would have been, if he had not insulated his loft.
$£$ $\qquad$
(Total 3 marks)
2. In a sale, normal prices are reduced by $20 \%$.

## SALE 20\% OFF

Andrew bought a saddle for his horse in the sale.
The sale price of the saddle was $£ 220$.
Calculate the normal price of the saddle.
$£$ $\qquad$
(Total 3 marks)
3. Hajra's weekly pay this year is $£ 240$

This is $20 \%$ more than her weekly pay last year.
Bill says 'This means Hajra’s weekly pay last year was $£ 192$ '.
Bill is wrong,
(a) Explain why.
$\qquad$
$\qquad$
(b) Work out Hajra's weekly pay last year.
4. The price of all rail season tickets to London increased by $4 \%$.
(a) The price of a rail season ticket from Cambridge to London increased by $£ 121.60$ Work out the price before this increase.
£ $\qquad$
(b) After the increase, the price of a rail season ticket from Brighton to London was £2828.80
Work out the price before this increase.
£
5. In a sale, normal prices are reduced by $25 \%$.

The sale price of a saw is $£ 12.75$
Calculate the normal price of the saw.
$£$
(Total 3 marks)
6. In a sale, normal prices are reduced by $12 \%$.

The sale price of a DVD player is $£ 242$.
Work out the normal price of the DVD player.

## Converting Recurring Decimals to Fractions

## Things to remember:

1. Call the recurring decimal " $x$ ";
2. Multiply $x$ by $10^{n}$ where $n$ is the number of recurring decimal digits;
3. Subtract $x$ from $10^{n} x$;
4. Divide by the coefficient of $x$;
5. Simplify the fraction if possible.

## Questions:

1. (a) Change $\frac{3}{11}$ to a decimal
(b) Prove that the recurring decimal $0 . \dot{3} \dot{9}=\frac{13}{33}$
2. Prove that the recurring decimal $0 . \dot{4} \dot{5}=\frac{15}{33}$
3. Express the recurring decimal 0.213 as a fraction
4. Prove that $0.47 \dot{7}$ can be written as the fraction $\frac{469}{990}$
5. Prove that the recurring decimal $0 . \dot{1} \overline{7}=\frac{17}{99}$
6. Express $0 . \dot{2} 7$ as a fraction in its simplest form.

## (Total 3 marks)

7. Change the recurring decimal $0 . \dot{2} \dot{3}$ to a fraction.
8. (i) Convert the recurring decimal $0 . \dot{3} \dot{6}$ to a fraction.
(ii) Convert the recurring decimal $2.13 \dot{6}$ to a mixed number. Give your answer in its simplest form.
9. Convert the recurring decimal $2.1 \dot{4} \dot{5}$ to a fraction.
10. Express the recurring decimal $0.12 \dot{6}$ as a fraction.
11. Express $0.3 \dot{2} \dot{8}$ as a fraction in its simplest form.
(Total 3 marks)
12. The recurring decimal $0 . \dot{7} \dot{2}$ can be written as the fraction $\frac{8}{11}$ Write the recurring decimal $0.57 \dot{2}$ as a fraction.
13. Express the recurring decimal $2.0 \dot{6}$ as a fraction.

Write your answer in its simplest form.

